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# Thermodynamics and kinetics of fluoride removal from simulated zinc sulfate solution by La(III)-modified zeolite

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**Abstract:** To understand the mechanism of fluoride removal from the simulated zinc sulfate solution by the La(III)-modified zeolite, the adsorbent was characterized by XRD, SEM and EDS. The effects of absorbent dose and contact time, the adsorption isotherms and the sorption kinetics were investigated. The experimental results were compatible with the Langmuir isotherm model. The theoretical maximum adsorption capacities are 20.83 and 23.04 mg/g at 303 and 313 K, respectively. And the physisorption is revealed using the Temkin isotherm model and the D–R isotherm model. The sorption process is more suitable by the pseudo-second-order kinetic models. Thermodynamic parameters such as standard free energy change ( $\Delta G^{\circ}$ <0 kJ/mol), standard enthalpy change ( $\Delta H^{\circ}$ =8.28 kJ/mol) and standard entropy change ( $\Delta S^{\circ}$ =0.030 kJ/(mol·K)) indicate the spontaneity of adsorption and endothermic physical sorption. Furthermore, the fluoride concentration in the industrial zinc sulfate solution decreases from 98.05 to 44.09 mg/L with the adsorbent dosage of 15 g/L.

Key words: La(III)-modified zeolite; fluoride removal; zinc sulfate solution; adsorption isotherm; kinetics

# 1 Introduction

Zinc is an important non-ferrous metal in modern society, and over 80% of zinc is produced through the conventional hydrometallurgical method with oxidative roasting, acid leaching, purification, and electrowinning process(OLPE) [1]. With poor mineral reserves, ores, including zinc, struggle with the "lean, fine, miscellaneous" dilemma. In practice, the roasting and leaching processes are combined, resulting in high fluoride ion concentration in electrolyte. It can cause problems in the electrowinning system, such as anode corrosion, cathode corrosion, zinc sticking, electrolytic zinc grade reduction [2,3]. In addition, high fluoride content can also worsen the working environment and damage the workers' health. So, the fluoride ion concentration in electrolyte needs to be reduced before reaching the electrowinning system (F<80 mg/L) [4]. In China, the fluoride concentration in the zinc electrowinning process is amended to be 50 mg/L [5].

Currently, pyrometallurgical roasting and caustic washing are widely applied to the removal of fluoride in

former requires high-temperature industry. The equipment, such as multiple hearth furnaces and rotary kilns, and there are disadvantages of high cost, high energy consumption and low efficiency, while the latter produces large amounts of wastewater and the waste water must be treated by other methods [6]. There are also other ways for fluoride removal, such as chemical precipitation [7], ion exchange [8], coagulation precipitation [9] and adsorption [10]. Coagulation precipitation is difficult to be widely used in practice because of the high cost and a quite long time for treatment [5]. Ion exchange is inefficiency and high zinc loss for removing fluoride from the zinc sulfate solution. Meanwhile, it will produce large number of wastewater containing fluoride, which needs to be further treated [11]. Chemical precipitation is a traditional method to remove the fluoride, but the property of fluoride removal is limited due to performance of poor filtration [12]. In addition, silicone and some resins as adsorbents are capable of removing fluoride [13]. However, other ions in the electrolyte will be lost because of their poor selectivity.

Zeolite is microporous aluminosilicates with threedimensional structure, which contains a lot of channels and pores. And it is lower price, abundance, diversity and molecular sieving [14]. So, it has been the focus of removing cationic and anionic ion. But its adsorption capacity is restrictive when it is used to remove anionic ion in the solution. And the positive ions within the channels and pores on the network are easily exchanged by other cations [15]. Therefore, to give place to active sites for the removal of fluoride and utilize stronger cationic-exchange properties, the polyvalent metals (e.g., La, Al, Zr, etc) were used to modify the zeolite to increase adsorption capacity [16,17]. Especially, lanthanum could form stable compounds with most non-metallic elements, so the La(III)-modified adsorbents will adsorb larger numbers of anionic ions [18]. Due to lower cost compared with other rare earth elements [19] and environmental friendly, nontoxic, the La(III)-modified zeolite was adopted to remove anionic ion in drinking water [17].

Therefore, the La(III)-modified zeolite was applied to removing the fluoride from the simulated zinc sulfate solution and exhibited good property in the previous studies. But compared with the efficiency of fluoride removal in drinking water, defluorination efficiency in zinc sulfate solution is limited. In this study, the common La(III)-modified zeolite fluoride removal adsorbent for the simulated zinc sulfate solution was prepared through the impregnating method. The thermodynamic and kinetic parameters were estimated. And the isotherm models and the kinetics models were investigated. The purpose is to understand the defluoridation behavior and the La(III)-modified zeolite mechanism and increase efficiency of fluoride removal from zinc sulfate solution with the La(III)-modified zeolite.

# 2 Experimental

# 2.1 Materials

The artificial zeolite sample in particle size of 850–425 µm was obtained from Sinopharm Chemical Reagent Co., Ltd., China. The sample was handled twice in deionized water at room temperature for 30 min while stirring, then filtered and dried to finish the sample pretreatment. The pre-process sample was also soaked in a 150 g/L La(NO<sub>3</sub>)<sub>3</sub> solution at 40 °C for 4 h with a solid to solution ratio of 1:5 while stirring and then immersed at room temperature for 20 h. After filtering and drying, the La(III)-modified zeolite sample was obtained.

# 2.2 Batch adsorption studies

Preparation of the simulated solution (100 mg/L  $F^-$ , 160 g/L  $Zn^{2+}$ , 240 g/L  $SO_4^{2-}$ ) was done by dissolving 0.221 g anhydrous sodium fluoride and 715 g  $ZnSO_4\cdot 7H_2O$  in 1 L of deionized water for practical application. Then, the adsorbent with different doses was

added into 100 mL of the stock solution in a glass conical flasks shaked in a thermostat water bath cauldron at a invariable speed of 150 r/min at 40 °C for 30 min. The effect of contact time ranging from 0.5 to 38 h on defluoridation was executed and the adsorption kinetics was studied in the same range of contact time. The adsorption isotherm was discussed with the initial fluoride concentrations of 20, 50, 80, 100, 150, and 200 mg/L at 30 and 40 °C at 150 r/min for a desired time. The thermodynamic parameters were estimated in the stock solution at 30, 35, 40, and 50 °C. And all experiments were performed at pH 4.59±0.02. Fluoride concentration was measured in filtrates after fluoride removal and filtering. The adsorbed fluoride capacity was estimated from

$$q_{\rm e} = (\frac{\rho_0 - \rho_{\rm e}}{m})V \tag{1}$$

where  $q_e$  is the adsorption capacity at equilibrium,  $\rho_0$  and  $\rho_e$  are the initial and equilibrium fluoride concentrations in the solution, respectively, V is the volume of the solution, and m is the mass of the adsorbent used.

The efficiency  $(\eta)$  of fluoride ion removal by the adsorbent was defined as

$$\eta = \left(\frac{\rho_0 - \rho_e}{\rho_0}\right) \times 100\% \tag{2}$$

# 2.3 Characterization

The phase of the adsorbent material was performed by X-ray diffraction (XRD, Rigaku3014) with  $Cu/K_{\alpha}$  radiation and scans were recorded from 10° to 75° (2 $\theta$ ). A high qualitatively scanning electron microscope (SEM) was used to exam the surface morphology of the zeolite and La(III)-modified zeolite. The spot elemental analyses of the zeolite and La(III)-modified zeolite were carried out using the energy dispersive X-ray spectroscopy (EDS) detector (SEM-EDS, JSM-6360LV, JEOL), respectively.

#### 2.4 Methods of analysis

Fluoride analysis was determined by ion-selective electrode method using an ion meter (PXSJ-216, Shanghai, Leici, China) with the fluoride ion selective electrode (PF-2-01, Shanghai, Leici, China). The triammonium citrate solution buffered the and background ion concentrations during measurement. pH was measured using the same ion meter with a pH electrode (E-201-C, Shanghai, Leici, China). Fluoride standard solutions with fluoride concentration ranges of 10-200 mg/L were used to obtain standard curves. The solution in the glass beaker was placed on a magnetic stirrer during measurement, while the electrode was placed in the solution. The fluoride analysis ended upon stabilization of the numerical reading displayed on the ion meter screen.

# 2.5 Fluoride removal from zinc sulfate electrolyte

The zinc sulfate electrolyte was collected from Yunnan Chihong Zn&Ge Co., Ltd., China. The composition of the electrolyte was measured, and the analyzed parameters were pH 4.95, Zn<sup>2+</sup> concentration 125.17 mg/L, Fe<sup>2+</sup> concentration 1.8 mg/L and F concentration 69.48 mg/L. To increase the fluoride concentrations of this electrolyte sample, the anhydrous sodium fluoride was added to the zinc sulfate electrolyte. The fluoride concentration was also raised by approximately 100 mg/L. The new sample was re-analyzed and reached 98.05 mg/L. The spiked electrolyte sample was treated with various adsorbent doses from 0.5 g to 1.5 g at the same contact time in different conical glass flasks, where 100 mL of the new sample was taken and mixed. After the defluoridation experiment, the solution was filtered from the solid adsorbent. Finally, the remaining fluoride in the filtrate was analyzed.

#### 3 Results and discussion

#### 3.1 Characterization

The XRD pattern of the La(III)-modified zeolite sample is exhibited in Fig. 1. The characteristic peaks of zeolite are observed at  $2\theta$ =15.78°, 20.33°, 23.78°, 26.28°, 29.93° and 36.64°. The XRD diffraction shows

the peaks of La<sub>2</sub>O<sub>3</sub> at  $2\theta$ =38.07°, 46.08°. The diffraction peaks at  $2\theta$ =35.50° and 41.99° are attributed to La<sub>2</sub>Si<sub>2</sub>O<sub>7</sub>. And other peaks are SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub> and Na<sub>2</sub>Si<sub>3</sub>O<sub>7</sub>. Figures 2(a) and (c) exhibit the SEM images of the zeolite and La(III)-modified zeolite. Compared with the zeolite, many small particles appeared on the surface of the La(III)-modified zeolite. Figure 2(b) shows the presence of Na, Mg, Al, Si, O on the surface of the zeolite. At the same time, Fig. 2(d) shows lanthanum except the original elements on the surface of the zeolite, which can be attributed to the soaking process with La(NO<sub>3</sub>)<sub>3</sub> salt solutions. Therefore, the La(III)-modified zeolite is obtained successfully.

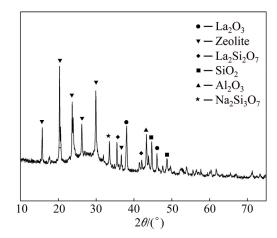


Fig. 1 XRD pattern of La(III)-modified zeolite sample

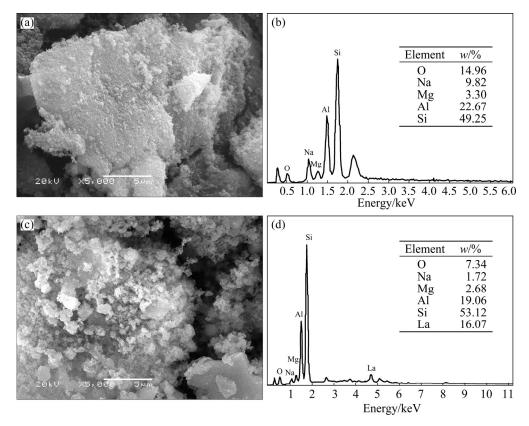


Fig. 2 SEM images (a, c) and EDS results (b, d) of zeolite (a, b) and La(III)-modified zeolite (c, d)

#### 3.2 Effect of adsorbent dose

The effect of absorbent dose was studied at a certain initial fluoride concentration of 100 mg/L, and the result is shown in Fig. 3. It is found that the fluoride removal rate increases from 33.54% to 40.49% with an increase in adsorbent dose from 5 to 17.5 g/L after 30 min, respectively. And the fluoride removal rate increases quickly with the adsorbent dose increasing from 5 to 10 g/L. Moreover, the adsorbent dose over 10 g/L, the increase of fluoride removal is negligible and almost achieves adsorption equilibrium. Thus, 10 g/L of adsorbent (La(III)-modified zeolite) is fixed as the optimum dose which could reach reasonably good defluoridation efficiency.

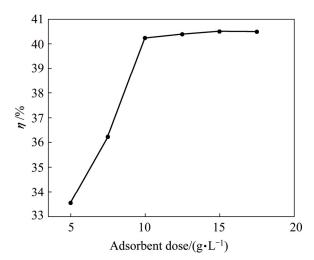


Fig. 3 Fluoride removal in simulated solution with different adsorbent (La(III)-modified zeolite) doses at  $(313\pm1)$  K and pH  $(4.59\pm0.02)$ 

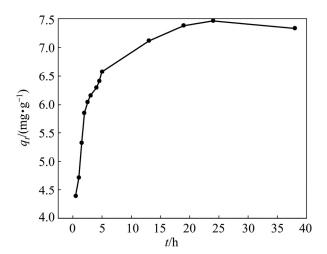
#### 3.3 Adsorption capacity versus contact time

The contact time is one of the critical factors in the defluoridation process. It is researched in the range of 0.5–38 h with a dose of 10 g/L at 150 r/min and the result is presented in Fig. 4. Figure 4 indicates that the defluoridation process can be divided into two parts. From 0.5 to 3 h, the adsorption capacity of fluoride increases from 4.39 to 6.57 mg/g. After 3 h, the growth rate of the adsorption capacity of fluoride slows down and then reaches balance time at 19 h. Hence, the optimum time is fixed as 19 h.

# 3.4 Adsorption isotherms

Adsorption isotherms, either through theoretical or empirical equations, are essential in the basic design and operation of adsorption processes. In the present study, Langmuir, Freundlich, Temkin and Dubinin–Radushkevich (D–R) isotherm models were introduced to evaluate the mechanisms of adsorption and the

maximum adsorption capacity of the adsorbent in a solid/liquid adsorption system [20]. The corresponding data are shown in Fig. 5, Tables 1 and 2.



**Fig. 4** Effect of contact time on fluoride removal with adsorbent (La(III)-modified zeolite) dose of 10 g/L at  $(313\pm1)$  K and pH  $(4.59\pm0.02)$  in simulated solution

The Langmuir isotherm model (Eq. (3)), which is based on monolayer adsorption on the homogeneous adsorbent surface without interaction between adsorbed molecules [21], is given as

$$\frac{1}{q_{\rm e}} = \frac{1}{q_{\rm m}} + \frac{1}{q_{\rm m}f\rho_{\rm e}} \tag{3}$$

where  $q_{\rm m}$  is the maximum amount of La(III)-modified zeolite for a complete monolayer on the bound surface, and f is a constant related to the affinity of the binding sites. As shown in Table 1, the  $q_{\rm m}$  and f values are calculated from the intercept and slope of the  $1/\rho_{\rm e}$  vs  $1/q_{\rm e}$  plots at 303 and 313 K (Fig. 5(a)). The separation factor ( $R_{\rm L}$ ) of Langmuir adsorption determines whether the adsorption is favorable. It can be obtained using (Eq. (4)) [22]:

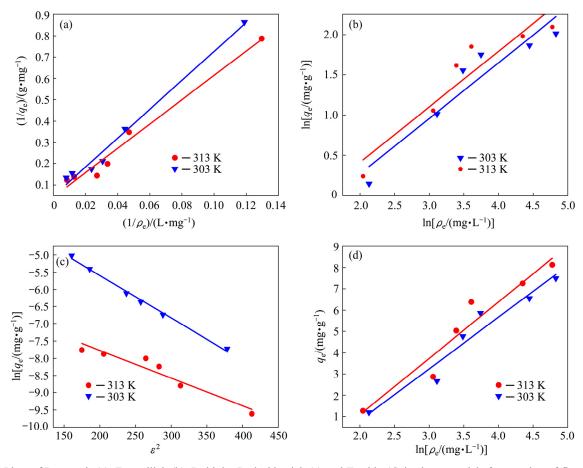
$$R_{\rm L} = \frac{1}{1 + f\rho_0} \tag{4}$$

where  $\rho_0$  is an important parameter to adsorption system prediction.

The Freundlich model (Eq. (5)) is an empirical equation based on the assumption of adsorption on the heterogeneous surface and multilayer adsorption with energetic, non-uniform distribution [23]. The model is given as

$$\ln q_{\rm e} = \ln K_{\rm F} + \frac{1}{n} \ln \rho_{\rm e} \tag{5}$$

where  $K_F$  and n are Freundlich constants related to



**Fig. 5** Plots of Langmuir (a), Freundlich (b), Dubinin–Radushkevich (c) and Temkin (d) isotherm models for sorption of fluoride on La(III)-modified zeolite at different initial fluoride concentrations with adsorbent dose of 10 g/L at (303±1) K and (313±1) K and pH (4.59±0.02) in simulated solution

Table 1 Different isotherm parameters for adsorption of fluoride ions on La(III)-modified zeolite at (303±1) and (313±1) K

T/K	Langmuir				Freundlich			
	$q_{\rm m}/({\rm mg}\cdot{\rm g}^{-1})$	$f/(L \cdot mg^{-1})$		$R^2$	$K_{\rm F}/({\rm mg}\cdot{\rm g}^{-1})$	n	$R^2$	
303	20.83	0.00	071	0.986	0.3286	1.4479	0.902	
313	23.04	0.00	)76	0.978	0.3799	1.4491	0.890	
T/K	D-R				Temkin			
1/ <b>K</b>	$Q_{\mathrm{D}}/(\mathrm{mol}\cdot\mathrm{g}^{-1})$	$B_{\rm D}/({\rm mol\cdot kJ}^{-2})$	$E/(kJ \cdot mol^{-1})$	$R^2$	$A_T/(\mathbf{L}\cdot\mathbf{g}^{-1})$	$B_T/(kJ \cdot mol^{-1})$	$R^2$	
303	0.0442	0.012	6.455	0.995	0.1898	2.423	0.945	
313	0.00212	0.008	7.906	0.922	0.2044	2.644	0.935	

**Table 2** Values of  $R_L$  obtained from Langmuir constant f at different initial fluoride concentrations for La(III)-modified zeolite at (303±1) and (313±1) K

// I =1\	$R_{ m L}$				
$\rho_{(\mathrm{F}^{-1})}/(\mathrm{mg}\cdot\mathrm{L}^{-1})$	303 K	313 K			
20	0.8757	0.8681			
50	0.7380	0.7246			
80	0.6378	0.6219			
100	0.5747	0.5681			
150	0.4843	0.4673			
200	0.4132	0.3968			

adsorption capacity and absorption intensity, or surface heterogeneity, respectively. As shown in Table 1, the  $K_{\rm F}$  and 1/n values are calculated from the intercept and slope of the  $\ln \rho_{\rm e}$  vs  $\ln q_{\rm e}$  plots at 303 and 313 K (Fig. 5(b)).

A comparison of the correlation coefficient  $(R^2)$  values of the Langmuir  $(R^2=0.978 \text{ and } 0.986)$  and Freundlich plots  $(R^2=0.902 \text{ and } 0.890)$  reveals that the former model is more suitable for the experimental data than the latter isotherm model, demonstrating favorable monolayer uniform adsorption conditions. Based on the Langmuir isotherm model, the predicted theoretical

maximum adsorption capacities of monolayer fluoride ion for La(III)-modified zeolite are 20.83 and 23.04 mg/g at 303 and 313 K, respectively. To access the fluoride removal efficiency of the La(III)-modified zeolite, a comparison of the Langmuir monolayer capacity of the present adsorbent is shown in Table 3 with some other reported materials. For  $0 \le R_L \le 1$ , the adsorption system will also be favorable, but it will be unfavourable when the  $R_{\rm L}$  exceeds 1. Linear adsorption can be supported for  $R_L=1$ , and irreversible adsorption for  $R_L=0$  [31].  $R_L$ values from Table 2 increased along with the decrease of adsorbent temperature and initial fluoride concentration, suggesting an increasing affinity between fluoride and adsorbent. All R<sub>L</sub> values ranged from 0 to 1, indicating favorable Langmuir adsorption. For the Freundlich isotherm model, the values of 1/n at 303 and 313 K are between 0 and 1, suggesting the favorable fluoride adsorption of the adsorbent. The values of  $K_F$  increased along with increasing temperature, showing that the fluoride adsorption capacity of the adsorbent increased along with the reaction temperature.

A comparison of the Langmuir and Freundlich isotherm models indicates that the fluoride ions were adsorbed at the monolayer region of the homogeneous adsorbent surface, thus achieving maximum adsorption capacity. However, the adsorption energy could not be calculated. The Dubinin–Radushkevich (D–R) isotherm

model (Eq. (6)), which predicts whether the adsorption is physisorption or chemisorptions [32], is expressed as

$$\ln q_{\rm e} = \ln Q_{\rm D} + B_{\rm D} \varepsilon^2 \tag{6}$$

$$\varepsilon = RT \ln(1 + \frac{1}{\rho_{\rm e}}) \tag{7}$$

$$E = (2B_{\rm D})^{-0.5} \tag{8}$$

where  $Q_D$  is the maximum adsorption capacity of the La(III)-modified zeolite,  $B_D$  is a coefficient related to mean sorption energy given by Eq. (6), and  $\varepsilon$  is the Polanyi potential obtained by Eq. (7).  $B_D$  can be used to estimate the free energy (E) of La(III)-modified zeolite, which is followed as Eq. (8).

The  $Q_{\rm D}$  and  $B_{\rm D}$  values are calculated from the intercept and slope of the  $\ln q_{\rm e}$  vs  $\varepsilon^2$  plots at 303 and 313 K (Fig. 5(c)) and shown in Table 1.The high correlation coefficients ( $R^2$ =0.995 and 0.922) reflect the compatibility of the experimental data with the D–R isotherm model. Defined as the free energy change (E) when 1 mol of fluoride ion shifts to the surface of the adsorbent from the solution, the values of E are found to be 6.455 and 7.906 kJ/mol. If the E values fall below 8 kJ/mol, the adsorption process can be viewed as physical adsorption; when the E values rang from 8 to 16 kJ/mol, the adsorption process is an ion exchange [33]. In the current study, the values of E follow the former,

Table 3 Comparative assessment of Langmuir monolayer capacity  $(q_m)$  of La(III)-modified zeolite with some references available data for other adsorbents

Absorbent	$q_{ m m}/\left({ m mg}{ m g}{ m g}^{-1} ight)$	Experimental condition	Ref.
Layered aluminum-based composite	concentration: 124–220 mg/L		[24]
Lanthanum hydroxide modified magnetites	1.42	pH 7.8, 303 K, aqueous solutions, concentration: 1–30 mg/L	[18]
Iron(III)-tin(IV) mixed oxide	10.47	pH (6.4±0.2), 303 K, aqueous solutions, concentration: 10–50 mg/L	[25]
KMnO <sub>4</sub> -modified carbon	15.90	pH 2, 298 K, aqueous solutions, concentration: 5–20 mg/L	[26]
Montmorillonite	3.37	pH 6, 298 K, aqueous solutions, concentration: 2–120 mg/L	
Laterite	0.85	pH 7.5, 303 K, aqueous solutions, concentration: 10–50 mg/L	[28]
Magnetic-chitosan	22.49	pH (7.0±0.2), 293 K, aqueous solutions, concentration: 5–40 mg/L	[29]
Fe(III) modified zeolite	2.31	pH (6.7±0.3), room temperature, aqueous solutions, concentration: 5–40 mg/L	[30]
La(III)-modified zeolite	20.83	pH (4.59±0.02), 303 K, simulated zinc sulfate solution, concentration: 20–200 mg/L	This work
La(III)-modified zeolite	23.04	pH (4.59±0.02), 313 K, simulated zinc sulfate solution, concentration: 20–200 mg/L	This work

suggesting that the fluoride adsorption of La(III)-modified zeolite is physisorption because of the weak Van der Waals force.

The Temkin isotherm model (Eq. (9)) was studied to investigate the influence of indirect adsorbent– adsorbate relationship on adsorption isotherms. It can be written as follows [34]:

$$q_{\rm e} = B_T \ln A_T + B_T \ln \rho_{\rm e} \tag{9}$$

where  $A_T$  is the binding constant and  $B_T$ =RT/b, b is the Temkin constant related to adsorption heat. As shown in Table 1, the  $B_T$  and  $A_T$  values are calculated from the intercept and slope of the  $\ln \rho_e$  vs  $q_e$  plots at 303 and 313 K (Fig. 5(d)). Given that its correlation coefficients ( $R^2$ ) are better than those of the Freundlich isotherm, the Temkin model is more compatible with the adsorbent. The values of  $B_T$  are 2.423 and 2.644 kJ/mol at 303 and 313 K, respectively. The relationship between fluoride and adsorbent is weak because of the values of  $B_T$ <8. It is suggested that the adsorption process of fluoride ions is expressed as physisorption [35], And the  $B_T$  values (the heat of adsorption of fluoride) increase along with increasing temperature, indicating that adsorption of fluoride is endothermic adsorption [36].

# 3.5 Adsorption kinetics

The fluoride adsorption kinetics was studied to evaluate the mechanisms of fluoride adsorption by the La(III)-modified zeolite, which controls the adsorption step. And the pseudo-first-order, pseudo-second-order and intra-particle diffusion models are used to examine the experiment data at the initial fluoride concentration of 100 mg/L. Relevant data are shown in Fig. 6 and Table 4.

The pseudo-first-order kinetics is described by [37]

$$\ln(q_{\rm e} - q_t) = \ln q_{\rm e} - k_1 t \tag{10}$$

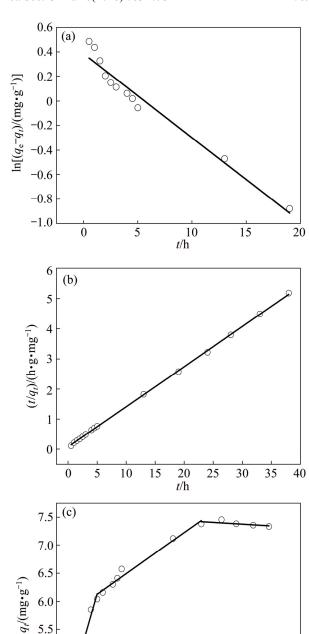
where  $q_t$  is the fluoride adsorption capacities of the La(III)-modified zeolite at time t, and  $k_1$  is the pseudo-first-order rate constant. As shown in Table 4, the pseudo-first-order rate constant  $(k_1)$  and  $q_e$  are found from the intercept and slope of the  $\ln (q_e - q_t)$  vs t plots at 313 K (Fig. 6(a)).

The pseudo-second-order rate equation is expressed as [37]

$$\frac{t}{q_t} = \frac{1}{k_2 q_e^2} + \frac{t}{q_e} \tag{11}$$

$$h = k_2 q_e^2 \tag{12}$$

where  $k_2$  is the pseudo-second- order rate constant, and h is the initial adsorption rate. As shown in Table 4, the pseudo-second-order rate constant  $(k_2)$  and  $q_c$  are calculated from the intercept and slope of the  $t/q_t$  vs t



**Fig. 6** Pseudo-first order (a), pseudo-second order (b) and intra-particle diffusion (c) kinetic models at initial fluoride concentration of 100 mg/L with 10 g/L La(III)-modified zeolite at (313±1) K and pH (4.59±0.02) in simulated solution

3

4

 $t^{1/2}/h^{1/2}$ 

5

7

6

2

5.0

4.5

plots at 313 K (Fig. 6(b)). In Table 4, the correlation coefficients ( $R^2$ ) of the pseudo-first-order and pseudo-second-order models are obtained as 0.960 and 0.999 respectively, exceeding 0.95. The  $k_1$  and  $k_2$  values are found to be 0.068 h<sup>-1</sup> and 0.224 g/(mg·h), respectively, that are far lower compared with those of drinking water. These values can be influenced by other ions of the simulated solution. However, the calculated  $q_e$  from the

**Table 4** Various kinetic parameters for fluoride adsorption on La(III)-modified zeolite at initial fluoride concentration of 100 mg/L at (313±1) K

$q_{\rm e(exp.)}/({\rm mg\cdot g^{-1}})$	Pseudo-first order			Pseudo-second order				
	$q_{\mathrm{e(cal.)}}/\mathrm{(mg\cdot g^{-1})}$	$k_1/\mathrm{h}^{-1}$	$R^2$	$q_{\mathrm{e(cal.)}}/(\mathrm{mg}\cdot\mathrm{g}^{-1})$	$k_2/(g\cdot mg^{-1}\cdot h^{-1})$	$h/(\text{mg}\cdot\text{g}^{-1}\cdot\text{h}^{-1})$	$R^2$	
7.379	1.468	0.068	0.960	7.507	0.224	12.626	0.999	

pseudo-first-order is lower than the experimental one, whereas that from the pseudo-second-order is closer to it. Hence, the fluoride adsorption of La(III)-modified zeolite and the experimental results are more suitable to the pseudo-second-order model. The maximum adsorption capacity from the pseudo-second-order model is less than that of the Langmuir isotherm because of the different initial fluoride concentrations. The initial adsorption rate is  $12.626 \ \text{mg/(g \cdot h)}$ .

While the pseudo-first-order and pseudo-secondorder models can describe the diffusion mechanism, the rate-limiting step of an adsorption process can be determined by the intra-particle diffusion model [32]. The rate constant for intra-particle diffusion can be predicted by

$$q_t = k_t t^{1/2} + C (13)$$

where  $k_i$  is the intra-particle diffusion rate constant, and C provides the boundary layer thickness. Intra-particle diffusion rate constant  $(k_i)$  and C are obtained from the intercept and slope of the  $q_t$  vs  $t^{1/2}$  plots at 313 K (Fig. 6(c)). If the plotted lines pass through zero, the intra-particle diffusion will define only the rate-controlling process [26]. However, the experimental data show all three lines; three steps exist in the adsorption process, including the initial curved portion, the intermediate linear portion, and a plateau. The linear fitting equations are presented as

$$q_t = 2.350t^{1/2} + 2.418 \quad (R^2 = 0.965, \text{ for } t \le 2)$$
 (14)

$$q_t = 0.472t^{1/2} + 5.379 \quad (R^2 = 0.973, \text{ for } 2 \le t \le 19)$$
 (15)

$$q_t = -0.041t^{1/2} + 7.597 \quad (R^2 = 0.187, \text{ for } t > 19)$$
 (16)

The first linear portion indicates the existing external surface adsorption. The rate constant ( $k_i$ ) and the boundary layer thickness (C) are obtained from the slope and the intercept of Eq. (14), and the values are 2.350 mg/(g·h<sup>1/2</sup>) and C=2.418 for t≤2. The second stage implies that the micro pore diffusion obtained at 2<t≤19, and the rate constant (0.472 mg/(g·h<sup>1/2</sup>)) is calculated from the slope of Eq. (15). The rate constant is lower than the first stage. The last stage shows that equilibrium adsorption can begin after 19 h, and C= $q_e$ =7.597 mg/g is closer to that of the pseudo-second order. The  $R^2$  values of the first two stages are high, which indicates that the data are fitted with the model. The  $R^2$  value of the last stage is low, although the data are already balanced. So,

the fluoride is transported by intra-particle diffusion into the particles and is adsorbed in the pores [26]. Nevertheless, the linear portion does not pass through the origin. This indicates that the fluoride adsorption onto La(III)-modified zeolite is rather complex process and that other possible rate-controlling steps exist.

# 3.6 Thermodynamic analysis

To investigate the influence of temperature on the defluorination process using La(III)-modified zeolite, different thermodynamic parameters, such as standard free energy change  $(\Delta G^{\Theta})$ , standard enthalpy change  $(\Delta H^{\Theta})$ , and standard entropy change  $(\Delta S^{\Theta})$ , are estimated as

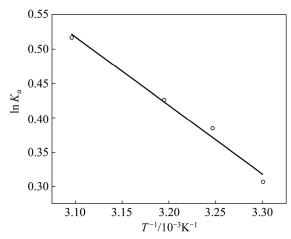
$$K_{\alpha} = \frac{q_{\rm e}}{\rho_{\rm e}} \tag{17}$$

$$\Delta G^{\Theta} = \Delta H^{\Theta} - T \Delta S^{\Theta} \tag{18}$$

$$\ln K_{\alpha} = \frac{\Delta S^{\Theta}}{R} - \frac{\Delta H^{\Theta}}{RT} \tag{19}$$

where  $K_a$  is the equilibrium constant, T is the thermodynamic temperature and R is the mole gas constant,  $\Delta S^{\Theta}$  is the standard entropy change,  $\Delta H^{\Theta}$  is the standard enthalpy change and  $\Delta G^{\Theta}$  is the standard free energy change. As shown in Fig. 7, the  $\Delta S^{\Theta}/R$  and  $\Delta H^{\Theta}/R$ values are calculated from the intercept and slope of the  $\ln K_a$  vs 1/T on the Van't Hoff plot. Table 5 shows the thermodynamic parameters at various temperatures. The correlation coefficients ( $R^2$ =0.985) from Fig. 7 reflects good linearity with the plot. The positive  $\Delta H^{\Theta}$  value the natural endothermic process suggests defluorination on La(III)-modified zeolite. For the enthalpy of adsorption, the values ranged from 8 to 25 kJ/mol, suggesting physical sorption, while the values that ranged from 83 to 830 kJ/mol indicate chemical sorption. According to the  $\Delta H^{\Theta}$  value in Table 5, the defluorination process is mainly physical sorption. The positive  $\Delta S^{\Theta}$  value also indicates increasing randomness during the defluorination step. This randomness may be explained by the increase of species at the solid-liquid interface from the release of aqua molecules and hydroxide ion when the fluoride ion is adsorbed [25,34]. The small and negative  $\Delta G^{\Theta}$  values indicate the natural adsorption spontaneity, while the increase of the  $\Delta G^{\Theta}$ with the decrease of temperature suggests that the defluorination process could be carried out difficultly at

lower temperatures [38]. So, the thermodynamic parameters indicate that the process of defluorination is spontaneous and endothermic.



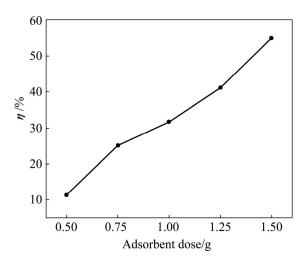
**Fig. 7** Plotting of  $\ln K_{\alpha}$  versus 1/T on fluoride adsorption by La(III)-modified zeolite

**Table 5** Thermodynamic parameters of sorption of fluoride on La(III)-modified zeolite

$\Delta S^{\Theta} /$	$\Delta H^{\Theta}$	$\Delta G^{\Theta}(\mathrm{kJ \cdot mol}^{-1})$			
$(kJ{\cdot}mol^{-1}{\cdot}K^{-1})$	$(kJ{\cdot}mol^{-1})$	303 K	308 K	313 K	323 K
0.030	8.28	-0.81	-0.96	-1.11	-1.41

### 4 Test with zinc sulfate electrolyte

To examine the result in zinc sulfate solution, La(III)-modified zeolite was applied to the zinc sulfate solution from the industry. Figure 8 shows the effect of fluoride ion removal from the zinc sulfate electrolyte sample (98.05 mg/L with added fluoride concentration). The defluorination efficiency clearly increases with the increase of the adsorbent dose. According to Fig. 8, with the adsorbent dose increasing from 5 to 15 g/L, the defluorination efficiency increases from 11.36% to



**Fig. 8** Fluoride removal in zinc sulfate electrolyte with different adsorbent doses by La(III)-modified zeolite at (313±1) K

55.01%. With the adsorbent dose of 15 g/L, the fluoride concentration decreases to 44.09 mg/L, which is below the industrial level of fluoride concentration (50 mg/L). Compared with the rate of the fluoride ion removal from the simulated zinc sulfate solution, the speed of fluoride removal from the zinc sulfate electrolyte sample is very slow. This might be because of the competing ions present in the zinc sulfate electrolyte sample and compete with the fluoride in the zinc sulfate electrolyte sample.

#### **5 Conclusions**

- 1) The La(III)-modified zeolite is performed by XRD, SEM, EDS, and the optimum adsorption conditions are determined. Under equilibrium, fluoride adsorption capacity exceeds 7 mg/g in the simulated solution (initial fluoride concentration of 100 mg/L).
- 2) The kinetic study suggests that the fluoride adsorption by La(III)-modified zeolite is compatible with the pseudo-second-order kinetic model, although the rate-limiting step is complex, as revealed by the intra-particle diffusion model.
- 3) The experimental data agree well to Langmuir isotherms model than the Freundlich, indicating monolayer uniform adsorption. And the theoretical maximum adsorption capacities were 20.83 and 23.04 mg/g at 303 and 313 K, respectively. The Dubinin–Radushkevich (D–R) and Temkin isotherm models suggest that the fluoride adsorption process is predominantly physisorption by the van der Waals force and fluoride removal is endothermic adsorption.
- 4) The values of  $\Delta H^{\Theta}$ ,  $\Delta S^{\Theta}$ , and  $\Delta G^{\Theta}$  reveal the natural spontaneity of defluorination by La(III)-modified zeolite and its endothermic process.
- 5) The adsorbent also decreases the fluoride concentration of the zinc sulfate electrolyte sample (98.05 mg/L with added fluoride concentration) to 44.09 mg/L with the dosage of 15 g/L. La(III)-modified zeolite successfully adsorbs fluoride from the zinc sulfate solution before the zinc electrowinning process.

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# La(III)改性沸石脱除模拟硫酸锌溶液中 氟离子的热力学和动力学

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摘 要:为了明确 La(III)改性沸石脱除模拟硫酸锌溶液中氟离子的机理,利用 XRD、SEM 和 EDX 对吸附剂进行表征,研究吸附剂用量和吸附时间对吸附过程的影响,采用吸附等温线与吸附动力学对吸附过程进行探究。结果表明,Langmuir 吸附等温线模型更适合吸附过程;在 303 和 313 K 条件下,吸附剂的最大理论吸附容量分别为 20.83 和 23.04 mg/g;Temkin 和 D-R 吸附等温线模型证明氟离子脱除过程为物理吸附,且吸附过程遵从准二级动力学模型;同时,热力学计算结果( $\Delta G^{\circ}$ <0 kJ/mol,  $\Delta H^{\circ}$ =8.28 kJ/mol,  $\Delta S^{\circ}$ =0.030 kJ/(mol·K))说明 La(III)改性沸石脱除模拟硫酸锌溶液中氟离子是自发、吸热的物理过程;将 La(III)改性沸石应用在工业硫酸锌溶液中,用量为 15 g/L 时,氟离子浓度从 98.05 mg/L 降低至 44.09 mg/L。

关键词: La(III)改性沸石; 脱氟; 硫酸锌溶液; 吸附等温线; 动力学

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