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Optimization of press bend forming path of aircraft integral panel

YAN Yu(阎昱), WAN Min(万敏), WANG Hai-bo(王海波), HUANG Lin(黄霖)

School of Mechanical Engineering and Automation, Beihang University, Beijing 100191, China

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Abstract: In order to design the press bend forming path of aircraft integral panels, a novel optimization method was proposed, which integrates FEM equivalent model based on previous study, the artificial neural network response surface, and the genetic algorithm. First, a multi-step press bend forming FEM equivalent model was established, with which the FEM experiments designed with Taguchi method were performed. Then, the BP neural network response surface was developed with the sample data from the FEM experiments. Furthermore, genetic algorithm was applied with the neural network response surface as the objective function. Finally, verification was carried out on a simple curvature grid-type stiffened panel. The forming error of the panel formed with the optimal path is only 0.098 39 and the calculating efficiency has been improved by 77%. Therefore, this novel optimization method is quite efficient and indispensable for the press bend forming path designing.

Key words: aircraft integral panel; press bend forming path; neural network response surface; genetic algorithm; optimization

1 Introduction

As a traditional forming method for aircraft integral panels, press bend forming possesses many advantages, such as low tooling cost, short cycle time and adaptability to different contours[1]. Based on the three-point bending principle, press bend forming process performs multi-step bending with universal dies according to planned paths to form single or compound curvature contours.

The critical factor to form the contour of the panels is the bending path, which includes the bending position and the punch displacement. In many aircraft companies, the planning of press bend forming path simply depends on the intuitions of the operators, who carry out numerous trial and error tests. Since the relation between the forming path and the objective shape is rather complicated and the flat panel is very expensive, the trial and error method will certainly lead to great loss of money and time. Therefore, the optimization of the press bend forming path is rather essential. Academic research on the optimization of metal forming process using FE simulations is gaining more and more attention. Many metal forming processes are considered: deep drawing[2-5], hydroforming[6-8], superplastic forming [9–10], extrusion[11], forging[12–14], and several other processes[15–16]. However, few attempts have been made to optimize the press bend forming of aircraft integral panels. A new method for solving this problem is proposed in this work.

Genetic algorithm(GA) is an adaptive search method based on Darwinian principles of natural selection, survival of the fittest, and natural genetic phenomena. With strong capability in optimizing functions with unknown dependence on design variables, GA has been widely used in many optimization problems[17]. GA is able to search very large solution spaces efficiently, since it uses probabilistic transition rules instead of deterministic ones and most effectively applied to problems in which small changes result in very nonlinear behavior in the solution space[18]. But, the optimization of press bend forming process by the GA method only is rather inefficiently numerous; runs of FEM analysis are needed; and each run of FEM simulation always takes several weeks.

The response surface methodology, RSM, is an optimization method which uses approximations of the objective and constraint functions. The approximations are based on functional evaluations at selected points in the design space[19]. By using the response surface to replace the iterations of FEM analyses, the optimization

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efficiency could be greatly enhanced. However, prediction based on the polynomial equation commonly used in RSM, is often limited to low levels, resulting in poor estimations of optimal formulations[20]. Artificial neural network(ANN) has a considerable capability of mapping the nonlinear relationship between the input and the output that cannot be efficiently predicted by analytical or conventional statistical models[21–22]. It has been proved that neural network response surfaces have higher precision than polynomial response surfaces [23–26].

The goal of this work is to develop an integrated approach using FEM equivalent model[27], artificial neural networks(ANN) and genetic algorithms(GA) for optimum path design of press bend forming. Then, an example is presented to verify this novel optimization method.

2 Theoretical background

2.1 BP neural network response surface

BP network is a feed-forward back propagation (BP) multilayer network. The artificial neurons are organized in layers with one or more intermediate hidden layers placed between the input layer and output layer, sending their signals "forward". First, the network obtains some information signals by the input layer; and the output produced from the first layer is then fed subsequently into the second layer and so on. The errors are then propagated backward[17]. The standard BP algorithm is

$$\begin{cases} y_i = f(\sum w_{ij}x_i + \theta) \\ f(x) = \frac{1}{1 + \exp(-x)} \\ w_{ij}(t+1) = w_{ij}(t) + \eta \delta_j y_j \\ \delta_j = \begin{cases} y_j(1-y_j)(T-y_j), j \text{ is output neuron} \\ y_j(1-y_j)\sum_k \delta_k w_{jk}, j \text{ is hidden neuron} \end{cases}$$
(1)

where *t* is the iteration number; x_i is the input of the neuron; y_i is the actual output of the neuron; $f(\bullet)$ is the Sigmoid function; θ is the bias of the neuron; w_{ij} is the connection weight of neuron *i* and neuron *j*; η is the learning rate; δ_j is the error of each neuron; and *T* is the expected output.

According to Kosmagoro theory, a three-layer BP network can approximate any continuous function when the proper structures and weights are provided. Therefore, in this work, a three-layer model using a back propagation(BP) algorithm is chosen.

The network adjusts its parameters by learning and training the data samples, by which the neural network's accuracy in foreseeing the performance is decided. So, it is crucial to determining the proper range of data to be used for training with a good experimental design method. Taguchi method uses a special set of arrays called orthogonal arrays to arrange experiments. These standard arrays stipulate the way of conducting the minimal number of experiments to give the full information of all the factors[28]. With this experimental design method, the calculation time can be greatly reduced and the "over learning" of the network can be avoided. Hence, FEM simulations are conducted according to the Taguchi experimental design method to gain the training data samples.

2.2 Genetic algorithm

The mathematical model of optimization generally consists of the objective function, design variables, the constraints, and the optimizing algorithm. The mathematical expression is

$$\begin{cases} \min f(x) \\ \text{s.t. } g_j(x) \leq 0 \text{ or } g_j(x) = 0, \ j = 1, 2, \cdots, m \\ x_{i\min} \leq x_i \leq x_{i\max}, i = 1, 2, \cdots, n \end{cases}$$
(2)

where f(x) is the objective function; *n* is the number of design variables; *m* is the number of the constraint function $g_j(x)$; $x_{i\min}$ and $x_{i\max}$ are the upper and the lower constraints of the design variable x_i , respectively.

The genetic algorithm based on natural selection is a method for solving both constrained and unconstrained optimization problems, and a process driving beiological evolution. It is well known that GA is able to find the global optimization point, and the results of this algorithm are more reliable than those of the common methods of optimization. Furthermore, it is good for optimizing the "Black Box" problem, such as the trained neural network.

The genetic algorithm repeatedly modifies a population of individual solutions. At each step, the genetic algorithm selects individuals at random from the current population to be parents and uses them to produce the children for the next generation. Over successive generations, the population "evolves" toward an optimal solution. The genetic algorithm uses three main types of rules at each step to create the next generation from the current population. Selection rules select the individuals, called parents, which contribute to the population at the next generation. Crossover rules combine two parents to form children for the next generation. Mutation rules apply random changes to individual parents to form children. The basic GA is expressed as follows:

$$SGA=(C, E, P_0, M, \Phi, \Gamma, \Psi, T)$$
(3)

where C is the coding method for individuals; E is the

fitness function for individuals; P_0 is the initial random population; M is the size of the population; Φ is the selection function; Γ is the crossover function; Ψ is the mutation function; and T is the stopping criteria.

2.3 Equivalent model of press bend forming

FEM analysis seems to be disabled in the press bend forming of integrally stiffened panel research, because of the complexity of the integral panel structures, the multi-step process and the limitations of the hardware. So, we created equivalent models[27] to conduct simulations and optimizations more efficiently.

Plastic equivalent plate is a plate made of a virtual material that forms the similar shape as the detailed model when being formed with the same bending path. The virtual material with special plastic characteristics is obtained by in-depth analysis of the bending and springback mechanics of the detailed models. The key factor in calculating the virtual material parameters is to ensure that both models yield at the same punch displacement and possess the same outer radius after springback. FEM simulation results indicate that at the same punch displacement, the error of equivalent model is less than 6%, while the efficiency of FEM simulation has been improved by 80%[27]. So, it is possible to plan the forming path with much less modeling and

calculation time than optimizing with the detailed models. The overall methodology for the forming path optimization of aircraft integral panels is shown in Fig.1.

3 Optimization of press bend forming path

3.1 Description of optimization problem

A workpiece is designed according to typical structures of the real aircraft panels, the length of which is 500 mm. The material is aluminum alloy 7B04-T7451. The radii of the punch and the die are both 35 mm, and the die gap is 100 mm, as shown in Fig.2.

Press bend forming is conducted at three positions, and the distances between the bending positions are 100 mm. The objective shape of this three-step forming is an arc with the radius of 1 430 mm and the centre angle of 16°. As shown in Fig.3, the whole arc represents the outer surface of the workpiece. With the three bending positions as the centers, three 160 mm-long (arc length) sections are chosen symmetrically to measure the arc heights. The arc heights are h_1 , h_2 and h_3 , which represent the arc heights of the three sections, respectively. From the geometry point of view, the ideal arc height of each section is: h=2.294 6 mm.

3.1.1 Objective function

The press bend forming error is taken as the



Fig.1 Flowchart of forming path optimization based on BP-GA algorithm



Fig.2 Sketch map of press bend forming process



Fig.3 Sketch map of press bend forming path optimization problem

objective function of this optimization problem, and the forming error is defined as

$$e_{\rm shape} = \sqrt{\Delta h_1^2 + \Delta h_2^2 + \Delta h_3^2} \tag{4}$$

where $\Delta h_1 = \left| \frac{h_1 - h}{h} \right|$ is the relative arc height error of

the left section; $\Delta h_2 = \left| \frac{h_2 - h}{h} \right|$ is the relative arc height

error of the right section; and $\Delta h_3 = \left| \frac{h_3 - h}{h} \right|$ is the

relative arc height error of the middle section.

3.1.2 Design of variables

Press bend forming is a multi-step forming process. If the bending positions of press bend forming are too close to each other, the influence among different bending steps could be so remarkable that the deformation areas may overlap each other. So, punch displacement at any position will make a contribution to the final shape. In order to get the symmetric shape, the punch displacement at the left and the right section should be the same. Assuming the side punch displacement as X_1 , and the middle punch displacement as X_2 , as shown in Fig.3, X_1 and X_2 are taken to be design variables of this optimization problem.

3.1.3 Constraints

The punch displacements commonly adopted in factories are around 5 mm. The one step press bend forming FEM model with the punch displacement of 3, 4, 5 and 6 mm are set up to choose the range of the punch displacement. The calculated arc heights are 1.12, 1.90, 2.71 and 3.55 mm, respectively. And buckling begins to appear on the stiffeners when the punch displacement reaches 6 mm. By considering both the ideal arc height and the forming quality, the constraints of the design

variables are selected:

$$\begin{cases} 0 < X_1 < 6 \text{ mm} \\ 0 < X_2 < 6 \text{ mm} \end{cases}$$
(5)

3.2 FEM modeling of multi-step press bend forming

FEM analysis techniques allow taking benefit from predictions of simulation methods to determine the optimal bend forming path. In order to enhance the calculation efficiency, an FEM equivalent model of press bend forming of integrally stiffened panels is established. When the material parameters of the plastic equivalent plate are calculated, Eq.(6) needs to be satisfied and the detailed model and the equivalent model should yield at the same punch displacement to get the same contours after springback:

$$R_{\rm 2E} = R_{\rm 2D} \tag{6}$$

where R_{2E} is the bending radius of the outer surface of the plastic equivalent plate after springback, and R_{2D} is the bending radius of the outer surface of the detailed model after springback[27]. The parameters of the virtual material calculated using the method proposed in our previous study[27] are as follows: the yield stress(σ_{sE}) is 303.397 MPa; the hardening exponent(n_E) is 0.629; and the hardening coefficient(K_E) is 1 220.213.

The simulations are carried out using the commercial code ABAQUS. Press bend forming is a multi-step forming process, and the springback takes place continually. In order to improve the simulation accuracy and avoid constantly transferring between the explicit and implicit algorithms, both the forming and springback processes are simulated with ABAQUS/Standard. The workpiece is modeled with solid elements C3D8R. The enhanced hourglass control approach is chosen. The tools are modeled with discrete rigid surfaces. As shown in Fig.4, by moving the punch and the dies, press bending and springback at different positions are accomplished.

3.3 Development of neural network response surface

The neural network response surface requires training with FEM experimental data to map the relationships between the punch displacements and the forming errors. The orthogonal test matrix $L_{25}(5^6)$ is adopted to carry out the experimental design. The side punch displacement X_1 and the middle punch displacement X_2 are taken as the two experiment factors, and the forming error e_{shape} defined in Eq.(4) as the experiment target. The factors and levels of the Taguchi method are shown in Table 1.

Twenty datasets are rationally selected to be training samples, and the other five datasets to be testing samples. Training is accomplished using the BP algorithm. A YAN Yu, et al/Trans. Nonferrous Met. Soc. China 20(2010) 294-301



Fig.4 Mises stress distribution of multi-step press bend forming process: (a) End of first bending; (b) End of first springback; (c) End of second bending; (d) End of second springback; (e) End of third bending; (f) End of third springback

1	5		0		
Feeter			Level		
Factor	1	2	3	4	5
Side punch displacement/mm	3.0	3.5	4	4.5	5
Middle punch displacement/mm	2.5	3.5	4	4.5	5

Table 1 Experimental layout of orthogonal test

three-layer network is developed, with the Tan-Sigmoid transfer function in the hidden layer and the linear transfer function in the output layer. The network should have two input neurons because there are two design variables. Five neurons are used in the hidden layer, as shown in Fig.5.

The Levenberg–Marquardt back propagation algorithm avoids computing Hessian matrix when modifying the second-order training speed. This algorithm appears to be the fastest method for training moderate-sized feedforward neural networks, thus LM is used for training. And the gradient descent with momentum weight and bias learning function (Learngdm) are used for learning. Learngdm calculates the weight change for a given neuron from the neuron's input and error, the weight (or bias), learning rate, and momentum constant, according to gradient descent with momentum. *MSE* is taken as the network performance function,



Fig.5 Topological structure of BP neural network

which measures the network's performance according to the mean of squared errors:

$$MSE = \frac{1}{N} \sum_{i=1}^{N} (e_i)^2 = \frac{1}{N} \sum_{i=1}^{N} (t_i - a_i)^2$$
(7)

where N is the total number of training dataset; t_i is the training sample data; and a_i is the output of the neural network. As shown in Fig.6, the training error decreases rapidly to the appointed range.

After the neural network is trained, its accuracy should be examined in response to untrained inputs so as to specify the network's accuracy in foreseeing the performance of the certain process. The five datasets that did not participate in the training are used to test the network. The outputs of the neural network and the Taguchi test results are shown in Table 2. It is observed that the relative errors for all the datasets are less than 6%, which means that the developed neural network is rather effective in mapping the relationship between the punch displacement and the press bend forming error



Fig.6 Training performance of neural network

 (e_{shape}) . Therefore, this neural network can appropriately substitute the time consuming FEM simulations in the GA optimization stage to enhance the optimization efficiency.

The trained neural network response surface is shown in Fig.7, in which the small circle marks represent the sample data, and the position pointed out by the arrow is the place where the press bend forming error (e_{shape}) gets the minimum value.

3.4 Optimization with genetic algorithm

Fitness function is used to convert the objective function value to the corresponding fitness value. With the M-file describing the objective function, the trained neural network response surface is defined as the fitness function for the GA optimization. Rank scaling function, stochastic uniform selection function, elite count reproduction function, and Gaussian mutation function are adopted as the GA options. In this work, the size of

Table	2	Contrast	between	the	output	of neur	al networ	k and	Taguchi	test	results

Tost number	V /mm	V /mm	$e_{ m sh}$	Relative error/%	
		A ₂ /11111	Taguchi test		
1	3.0	2.5	0.938 18	0.943 0	0.513 76
2	3.0	3.5	0.748 61	0.755 0	0.853 58
3	3.0	4.0	0.692 42	0.688 0	0.638 34
4	3.0	4.5	0.678 09	0.671 0	1.045 58
5*	3.0	5.0	0.708 61	0.691 1	2.471 03
6	3.5	4.0	0.461 75	0.454 6	1.548 46
7	3.5	4.5	0.448 19	0.455 3	1.586 38
8	3.5	5.0	0.500 76	0.514 1	2.663 95
9	3.5	2.5	0.771 56	0.757 7	1.796 36
10*	3.5	3.5	0.535 66	0.525 5	1.896 73
11	4.0	5.0	0.335 31	0.320 0	4.565 92
12	4.0	2.5	0.627 96	0.638 1	1.614 75
13	4.0	3.5	0.329 43	0.329 6	0.051 60
14	4.0	4.0	0.218 23	0.223 2	2.277 41
15*	4.0	4.5	0.219 78	0.218 2	0.718 90
16	4.5	3.5	0.240 99	0.227 6	5.556 25
17	4.5	4.0	0.078 06	0.098 5	0.563 67
18	4.5	4.5	0.125 82	0.114 0	1.446 51
19	4.5	5.0	0.300 10	0.308 5	2.799 07
20*	4.5	2.5	0.571 92	0.583 3	1.989 79
21	5.0	4.5	0.334 71	0.331 2	1.048 67
22	5.0	5.0	0.448 38	0.449 6	0.272 09
23	5.0	2.5	0.610 28	0.610 1	0.029 49
24	5.0	3.5	0.357 16	0.358 1	0.263 19
25*	5.0	4.0	0.297 92	0.296 5	0.476 64

The datasets with "*" marks are the testing datasets for the neural network, while the others are the training datasets.



Fig.7 Sketch map of neural network response surface

the initial population is 30, and the crossover rate is 0.8. The stopping criteria is reached when X_1 =4.47 mm, and X_2 =4.22 mm. The output of the neural network with this input is: e_{shape} =0.083 298.

3.5 Verification with FEM analysis

Verification of the optimal press bend forming path is carried out with both the FEM equivalent model and the FEM detailed model. The contrasts of the FEM analyses are shown in Table 3. According to the simulation results of the FEM equivalent model, it is obvious that the optimized path works much better than any press bend forming path used in the Taguchi test does. In addition, this optimal path also works well with the detailed model, and the forming error (e_{shape}) is only 0.098 39. The forming result indicates that the equivalent model performs quite well in the aspect of "equivalent", and the differences between the two models are less than 4.25%. The calculating efficiency of it has been improved by 77%.

As shown in Fig.8, not only the shape accuracy but also the surface quality is ensured by the optimal path of press bend forming. The surface of the stiffened panel is smooth with no buckling on the stiffeners, and the shape is well symmetrically formed.

Considering the width to thickness ratio, the bending deformations of the stiffener and the skin are narrow plate bending and wide plate bending, respectively.



Fig.8 Equivalent plastic strain distribution of detailed model: (a) Front view; (b) Isometric drawing

So, the stiffener is under the plane stress condition, while the skin is under the plane strain condition. Compared with the outer surface of the skin, the normal bending stress of the stiffener top is larger, as it is farther from the neutral surface. In addition, the compression stress from the punch is substantial. As a result, the plastic deformation appeared first at the stiffener top. Because the curvature of the aircraft wing panel is usually very small, the punch displacement is not large. Therefore, most of the material of the specimen does not experience plastic deformation, as shown in Fig.8. And the final curved shape is owing to the plastic deformation of the stiffeners.

4 Conclusions

1) The application of the FEM equivalent model ensures fast optimization of the bend forming path. Compared with the detailed model, the computation efficiency of the equivalent model has been improved by 77%, and the differences between the two models are less than 4.25%. Thus, the total calculation time of the FEM Taguchi experiments can be dramatically reduced.

2) The developed neural network response surface has a strong mapping ability for press bend forming process of aircraft integral panels. It acts as a good substitute for the time consuming FEM simulations in

Model	Minimum e _{shape} before optimization (Taguchi test)	e_{shape} after optimization	Left arc height after optimization/ mm	Middle arc height after optimization/ mm	Right arc height after optimization/ mm	FEM analysis CPU time/s
FEM equivalent model	0.078 06	0.036 03	2.347 62	2.323 04	2.351 21	3.92×10^4
FEM detailed model	-	0.098 39	2.451 98	2.320 96	2.454 21	1.68×10^{5}

the GA optimization, and achieves the goal of optimization with much less runs of FEM calculations.

3) The precise quantitative results of this study show that the FEM equivalent model, neural network response surface and their combination with the GA can realize the fast optimization of the press bend forming path, which is a pivotal problem in the aircraft integral panel manufacturing. Furthermore, this work provides a valuable research method for the optimization of other complicated forming processes.

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