

# AXIAL LOADS ACTING ON MANDREL IN COPPER RIFLED TUBE DRAWING PROCESS<sup>①</sup>

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**ABSTRACT** Stresses and axial loads acting on the mandrel in the copper rifled tube drawing process were analysed, and factors affecting on the axial loads on mandrel were discussed. Results show that the depth of the mandrel dragged into sizing zone and lubrication have major influence on drawing loads and fin shapes.

**Key words** drawing copper rifled tube lubrication fin

## 1 INTRODUCTION

In recent years, the rifled tube, i. e. a tube with spiral groove on its inner surface, is developed. The rifled tubes are widely used in heat exchangers of air conditioners and refrigerators because of their excellent heat transfer performance, compared with that of conventional copper bare tubes<sup>[1-3]</sup>. The rifled tube drawing is different from the conventional bare tube drawing in the mandrel itself rotating in the drawing process (see Fig. 1). Up to date, however, the analysis of axial loads on rotating mandrel has not been reported. In this paper, stresses and axial loads acting on the mandrel in the rifled tube drawing process were analysed and factors affecting on the axial loads on mandrel were discussed.

## 2 ANALYSIS

Fig. 2 shows external forces acting on the mandrel in the rifled tube drawing process. In order to analyse stresses acting on the mandrel, the following assumptions are made.

(1) The inner surface of the drawing tube are gradually contacted with the driving side of grooves of the rotating mandrel in the

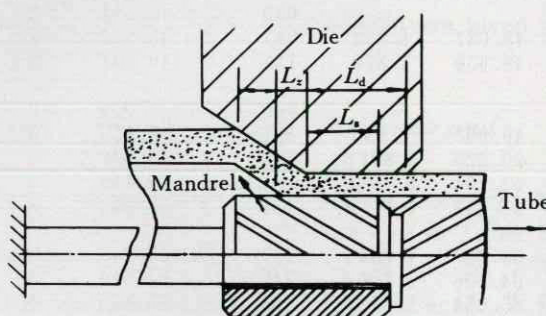


Fig. 1 Schematic illustration of the rifled tube drawing with spiral groove mandrel

drawing process.

(2) The normal pressure of the contacted side between the drawing tube and the groove is approximately  $p_r$ .

(3) The circumferential component  $p_t$  of  $p_r$  constitutes the driving moment of the rotating mandrel in the drawing process.

(4) The resistant moments are constituted from friction stresses and so on. It is shown in Fig. 2 that

$$\left. \begin{aligned} p_n &= p_r \times \cos \gamma, \quad p_b = p_n \times \cos \varphi, \\ p_t &= p_n \times \sin \varphi, \quad p'_b = \mu \times p_n \times \cos \varphi, \\ p'_t &= \mu \times p_n \times \sin \varphi \end{aligned} \right\} \quad (1)$$

where  $\gamma$ —groove top angle;  $\varphi$ —helix an-



gle;  $\mu$ —friction coefficient.

On basis of moment equilibrium of the rotating mandrel, it follows that

$$p_t \times S_3 \times r = (p'_t \times S_3 + \mu \times p_r \times S_2) r \quad (2)$$

where  $S_3 = K_3 \times N_z \times H_z \times L_z$ —side contact area between the driving side of the groove and the inner surface of tube;  $S_2 = K_2 \times \pi \times D_x \times L_z$ —contact area between the top of the groove and the inner surface of the tube;  $K_2 (< 1)$ —ratio of contact in  $S_2$ ;  $K_3 (< 1)$ —ratio of contact in  $S_3$ ;  $N_z$ —number of grooves;  $H_z$ —depth of groove;  $L_z$ —length of contact in the deformation zone;  $D_x$ —mean diameter of the drawn tube.

Substituting eqs. (1) into (2), then

$$P_b = p_r \times [\mu / (\operatorname{tg} \varphi - \mu)] \times (S_2 / S_3) = \mu' \times p_r \quad (3)$$

where

$$\mu' = [\mu / (\operatorname{tg} \varphi - \mu)] \times (S_2 / S_3) \quad (4)$$

On the basis of analysis of the forces acting on the mandrel in Fig. 2, the axial forces acting on the mandrel have  $P_b$ ,  $P'_b$ ,  $\mu \times P_r \times \sin \gamma$  and  $\mu \times P_r \times S_4$ , thus the axial load acting on the mandrel is obtained

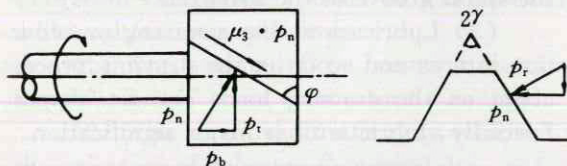


Fig. 2 Schematic representation of stress distribution in the mandrel

$$P_x = (P_b + P'_b) \times S_3 / \operatorname{tg} \varphi + \mu \times P_r (S_2 + S_4) = P_r [(\mu' + \mu \times \sin \varphi / \sin \gamma) S_3 / \operatorname{tg} \varphi + \mu (S_2 + S_4)] \quad (5)$$

where  $S_4 = \pi \times D_x \times L_s$ —contact area between the mandrel and the inner surface of the tube in the sizing zone;  $L_s$ —length of the mandrel dragged into sizing zone.

The drawing load in the deformation zone is<sup>[4]</sup>

$$P_c = \frac{\sigma_t \times (1 + B)}{B} \times \{1 + \frac{t_2}{t_1} [\frac{B \times \sigma_{za}}{\sigma_t \times (1 + B)} - 1]\} \times S \quad (6)$$

and

$$P_r = \frac{t_1^{(1+B)} - t_2^{(1+B)}}{t_1 - t_2} \times (1 - \frac{B \times \sigma_{za}}{1 + B} + \frac{\sigma_t}{B}) / t_1^B \quad (7)$$

where  $B = (\mu + \mu') / \operatorname{tg} \alpha$ ;  $\alpha$ —die semi-angle;  $\sigma_{za}$ —stress on exit in tube drawing<sup>[4]</sup>.

The drawing load acting on the sizing zone is

$$P_D = P_b \times S_4 \quad (8)$$

From eqs. (8) and (9), the drawing load is as follows:

$$P = P_c + P_D \quad (9)$$

### 3 EXPERIMENTAL

The annealed pure-copper bare tube of O. D. 9.52 mm and I. D. 8.72 mm is drawn into the rifled tube of O. D. 8.0 mm and I. D. 7.28 mm by tube drawing with fixed, spirally grooved mandrel. The rifle tube drawing are carried out with type WD-10 mechanical machine by the fixed, spirally grooved mandrel, of which the groove length is 2 mm, helix angle is 21°. The die semi-angle is 12°. The drawing load and axial loads acting on the mandrel are measured with strain gauges at the same time.

### 4 RESULTS AND DISCUSSION

Fig. 3 shows typical loads versus grips displacement curves for rifled tube with fixed mandrel. Fig. 4 shows influence of  $L_s$  on the drawing loads. Tables 1 and 2 show effect of  $L_s$  on the spiral raising angle ( $\varphi_s$ ) on tube inner surface and effect of friction on drawing loads.

It is shown in Fig. 4 that the deeper ( $L_s$ ) the mandrel dragged into sizing zone, the higher the drawing loads because of increasing friction stresses in the sizing zone. So the site ( $L_s$ ) of the mandrel in the sizing zone must be suitable. Otherwise, when  $L_s$  is excessive, the tendency of breakage in drawing tube increases; Or when  $L_s$  is too short, the fin shape of the tube may not fill into the spiral groove of the mandrel. Besides, lubrication, die an-



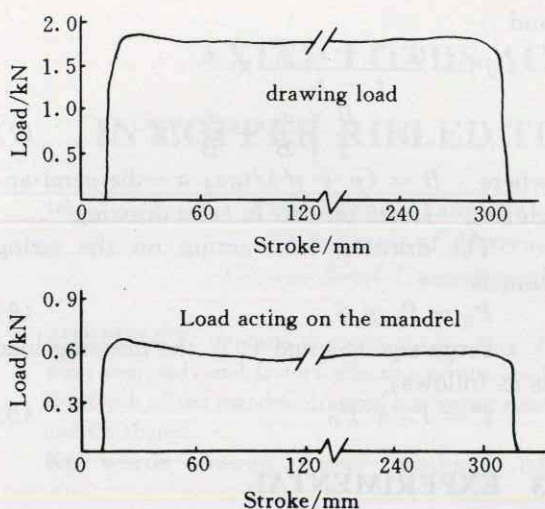


Fig. 3 Typical loads versus grips displacement curves for rifled tube with fixed mandrel

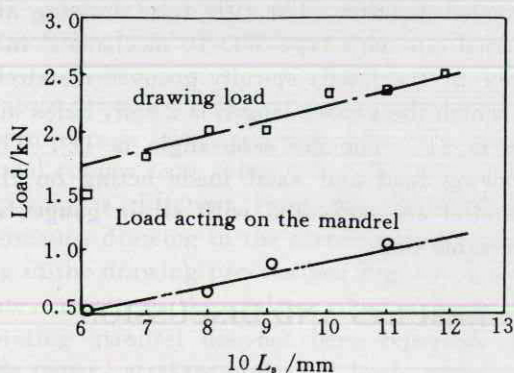


Fig. 4 Effect of  $L_s$  on drawing loads

Table 1 Effect of  $L_s$  on the spiral raising angle

No.	1	2	3	4
$L_s$ /mm	1.1	0.7	0.9	0.8
$\varphi_s$ /( $^\circ$ )	18.43	18.00	19.43	18.60
$H_z$ /mm	0.11	0.07	0.08	0.08
No.	5	6	7	8
$L_s$ /mm	1.2	0.5	1.0	1.1
$\varphi_s$ /( $^\circ$ )	24.56	10.60	21.82	21.80
$H_z$ /mm	0.12	0.05	0.09	0.11

Table 2 Effect of friction on drawing loads

Drawing	$L_s$ /mm	Lubrication condition	$\mu^*$	$P$ /N	$H_z$ /mm
$d$ 9.5 mm $\times$ 0.40 mm	1.1	dry	0.16	2 650	0.06
		mixed	0.12	1 950	0.07
$d$ 8.0 mm $\times$ 0.36 mm		wet	0.08	1 400	0.10

$\mu^*$  — reference value of friction coefficient<sup>[5]</sup>

gle, reduction in area and so on in the drawing process affect on the drawing loads and fin shapes. Specially, lubrication has major significance (see Table 2).

## 5 CONCLUSIONS

(1) The depth ( $L_s$ ) of the mandrel dragged into sizing zone and lubrication have major influence on drawing loads and fin shapes.

(2) The site ( $L_s$ ) of the mandrel in the sizing zone must be suitable. Otherwise, when  $L_s$  is excessive, the tendency of breakage in drawing tube increases; or when  $L_s$  is too short, the fin shape of the tube may not fill the spiral groove of the mandrel.

(3) Lubrication, die semi-angle, reduction in area and so on in the drawing process affect on the drawing loads and fin shapes. Specially, lubrication has major significance.

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(Edited by Peng Chaoqun)